

Digital Schoolhouse Puzzle Page

"If I had an hour to solve a problem I'd spend 55 minutes thinking about the problem and 5 minutes thinking about solutions"

Albert Einstein

Welcome to the Digital Schoolhouse Puzzle Page

On this paper, we will investigate a series of puzzles that can be used to promote Computational Thinking. This month we will investigate Knights and Knaves...

Knights and Knaves I

An island has two kinds of inhabitants, *knights*, who always tell the truth, and *knaves*, who always lie.

You go to the island and meet A and B.

A says "B is the knight"

B says "The two of use are of oppose types."

What types of inhabitants are A and B ?

Answer: Both are Knaves

Let p and q be the proposition statements that A is a knight and B is a knight, respectively. So, then $\neg p$ represents the proposition that A is a knave and $\neg q$ that B is a knave.

If A is a knight then p is true. Since knights always tell the truth, q must also be true.. Then the compound proposition statement $(p \sqcap \neg q) \vee (\neg p \sqcap q)$ would have to be true, but it is not. Thus, if A is a knight then B's statement must also be true, but it is not. So, A is not a knight and therefore must $\neg p$ be true.

If A is a knave, then B must not be a knight since knaves always lie. So, then both $\neg p$ and $\neg q$ hold since both are knaves.

Linkage to Computer Science

This puzzle is an example of propositional logic which underpins systems specification, and the design of logic circuits.

Solutions

7	2	9	5	4	3	5	6	2	7
3	1	8	6	9	7	2	5	4	3
9	3	5	4	1	2	2	8	6	3
4	4	9	7	1	6	8	5	9	3
8	3	3	2	4	1	9	4	7	2
5	6	5	1	9	4	4	2	2	1
8	7	4	4	2	1	3	9	6	5
2	4	3	6	9	8	7	3	9	5
6	8	5	1	7	4	3	3	7	2
9	1	7	3	5	2	4	4	8	6

Puzzle 42: (Hard, difficulty rating 0.72)

3	6	2	5	1	5	2	9	3	3
7	5	9	4	6	8	1	8	2	3
1	4	4	8	6	2	3	2	2	6
4	4	1	1	9	3	6	2	6	7
2	2	7	5	9	8	4	4	6	3
8	6	3	7	5	1	4	4	1	5
8	7	4	4	1	5	7	3	6	8
2	9	4	1	5	7	3	6	8	5
6	1	2	6	7	8	4	3	5	3
4	6	7	3	3	2	1	8	9	6

Puzzle 41: (Medium, difficulty rating 0.54)

9	3	5	6	1	7	8	2	2	4
7	6	4	8	5	2	1	9	6	3
2	1	8	2	4	3	9	6	6	5
3	2	3	6	1	8	4	8	7	9
4	5	4	7	6	6	3	2	2	8
6	1	9	8	7	7	8	1	9	6
2	1	5	8	7	3	9	6	9	4
7	9	6	1	4	2	5	3	3	8
8	3	4	9	6	5	2	7	1	1

Puzzle 40 (Easy, difficulty rating 0.39)

Puzzle 40: Easy

8		4				2	7	
7		6	1	4			3	
	4		5				1	
	8	2	3	9	6	7	4	
	5				1		2	
	6			5	8	4		7
	2	8				3		6

Puzzle 41: Medium

4	6	7				1		9
		2	6			4		
8					1			
2			1			3	6	
1				8				2
	8	5			3			4
			3					1
		1			4	6		
6	8					2	9	3

Puzzle 42: Hard

9	1		3					
6	8			7				2
	4	3		9				
			2	1	3			5
				9		7		
3			5	8	6			
				2		5	4	
4				6			1	3
					5		2	7